



Generalized Convexity and Generalized Monotonicity

By Nicolas Hadjisavvas

Springer Apr 2001, 2001. Taschenbuch. Book Condition: Neu. 235x155x22 mm. Neuware - A famous saying (due to Herriot) defines culture as 'what remains when everything is forgotten'. One could paraphrase this definition in stating that generalized convexity is what remains when convexity has been dropped. Of course, one expects that some convexity features remain. For functions, convexity of epigraphs (what is above the graph) is a simple but strong assumption. It leads to beautiful properties and to a field in itself called convex analysis. In several models, convexity is not present and introducing genuine convexity assumptions would not be realistic. A simple extension of the notion of convexity consists in requiring that the sublevel sets of the functions are convex (recall that a sublevel set of function a is the portion of the source space on which the function takes values below a certain level). Its first use is usually attributed to de Finetti, in 1949. This property defines the class of quasiconvex functions, which is much larger than the class of convex functions: a nondecreasing or nonincreasing one variable function is quasiconvex, as well as any one-variable function which is nonincreasing on some interval $(-\infty, a]$ or $(-\infty, a)$ and nondecreasing on its complement. Many other classes of generalized convex functions have been introduced, often for the needs of various applications: algorithms, economics, engineering, management science, multicriteria optimization, optimal control, statistics. Thus, they play an important role in several applied sciences. A monotone mapping F from a Hilbert space to itself is a mapping for which the angle between $F(x) - F(y)$ and $x - y$ is acute for any x, y . It is well-known that the gradient of a differentiable convex function is monotone. The class of monotone mappings (and the class of multivalued monotone operators) has remarkable properties. This class has been generalized in various directions, with applications to partial differential equations, variational inequalities, complementarity problems and more generally, equilibrium problems....



READ ONLINE
[4.7 MB]

Reviews

Unquestionably, this is the greatest operate by any article writer. I could comprehend everything out of this written e book. Your way of life span will be transform as soon as you total reading this book.

-- **Andy Erdman**

It is simple in study easier to comprehend. It is one of the most awesome ebook i have read through. You wont truly feel monotony at at any moment of your respective time (that's what catalogs are for concerning in the event you question me).

-- **Clint Sporer**